Math 55 Discussion problems 6 Apr

- 1. (a) Find a recurrence relation for the number of bit strings of length n that contain three consecutive 0s.
 - (b) What are the initial conditions?
 - (c) How many bit strings of length seven contain three consecutive 0s?
- 2. (a) Find a recurrence relation for the number of ways to completely cover a $2 \times n$ checkerboard with 1×2 dominoes. [Hint: Consider separately the coverings where the position in the top right corner of the checkerboard is covered by a domino positioned horizontally and where it is covered by a domino positioned vertically.]
 - (b) What are the initial conditions for the recurrence relation in part (a)?
 - (c) How many ways are there to completely cover a 2×17 checkerboard with 1×2 dominoes?
- 3. How many permutations of the 26 letters of the English alphabet do not contain any of the strings *fish*, *rat* or *bird*?
- 4. Find the number of solutions of the equation $x_1 + x_2 + x_3 + x_4 = 17$, where $x_i, i = 1, 2, 3, 4$, are nonnegative integers such that $x_1 \leq 3$, $x_2 \leq 4$, $x_3 \leq 5$, and $x_4 \leq 8$.
- 5. An integer is called squarefree if it is not divisible by the square of a positive integer greater than 1. Find the number of squarefree positive integers less than 100.
- 6. How many onto functions are there from a set with seven elements to one with five elements?
- 7. A small post office has only 4-cent stamps, 6-cent stamps, and 10-cent stamps. Find a recurrence relation for the number of ways to form postage of n cents with these stamps if the order that the stamps are used matters. What are the initial conditions for this recurrence relation?